

2021

## CHEMISTRY — HONOURS

First Paper

(Group - B)

Full Marks : 50

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.*

CHT-13a

Unit - I

Answer *any three* questions.

1. (a) The number of gas molecules of mass 'm' with speed between  $C$  and  $C + dC$  is given by

$$dN = AC^2 e^{-mC^2/2kT} dC$$

Calculate the value of 'A'.

How does the above distribution vary with temperature?  $\left( \text{Given: } \int_0^{\infty} x^2 e^{-ax^2} dx = \frac{1}{4} \sqrt{\frac{\pi}{a^3}} \right)$

- (b) Calculate the number of binary collision per  $\text{cm}^3$  per second in helium gas at  $27^\circ\text{C}$  and 1 atm. Given that the diameter of He atom =  $2 \times 10^{-8}$  cm. 3+2
2. (a) Write down the Maxwell distribution for molecular speed of gases in three dimensions and describe the features using graphical plot.
- (b) Use the Maxwell's distribution of molecular speed to estimate the fraction of  $\text{N}_2$  molecules at 500 K that have speeds in the range of  $290\text{--}300 \text{ ms}^{-1}$ . 3+2
3. (a) The virial equation of state in terms of  $P$  is given by (neglecting terms of higher order)

$$Z = 1 + \frac{1}{RT} \left( b - \frac{a}{RT} \right) P + \frac{a}{(RT)^3} \left( 2b - \frac{a}{RT} \right) P^2.$$

Set up an expression for the initial slope of 'Z' versus 'P' curve of a real gas and obtain an expression for the Boyle temperature of the gas.

- (b) Apply the equipartition principle to calculate  $\gamma = \frac{C_P}{C_V}$  for  $\text{N}_2\text{O}$  assuming it to be ideal. 3+2

Please Turn Over

4. (a) Derive the reduced equation of state for 'n' moles of a real gas obeying the van der Waals equation.  
 (b) Consider the following equation of state for a gas :

$$P\bar{V} = RT\left(1 + \frac{b}{\bar{V}}\right)$$

Would it be possible to liquefy the gas? Explain. 3+2

5. (a) What is Lennard-Jones 6-12 potential? Draw the Lennard-Jones potential against the internuclear distance plot.  
 (b) At normal temperature, iodine is a solid but fluorine is a gas. Explain. 3+2

### Unit - II

Answer *any two* questions.

6. (a) Identify the extensive and intensive properties among the following :  
 free energy, molar entropy, heat capacity, pressure.  
 (b) Calculate Q, W,  $\Delta E$  and  $\Delta H$  when one mole of ideal gas is reversibly expanded from 10 atm pressure and 2 lit to 5 atm isothermally at 27°C. 2+3
7. (a) Show that  $\left(\frac{\partial E}{\partial V}\right)_T = 0$  for an ideal gas.  
 (b) Calculate the enthalpy of formation of  $\text{NH}_3$ , given the enthalpy of combustion of  $\text{NH}_3$  and  $\text{H}_2$  are  $-90.6 \text{ kcal mol}^{-1}$  and  $-68.3 \text{ kcal mol}^{-1}$  respectively. 2+3
8. (a) Derive the integrated form of Kirchhoff's equation to show the variation of  $\Delta H^\circ$  of a reaction with temperature. Under what condition this variation becomes independent of temperature?  
 (b) The heat capacity of a substance is often given by :

$$\bar{C}_p = a + bT + \frac{C}{T^2}$$

Use this expression to estimate the change in molar enthalpy of carbon dioxide when heated from 20°C to 40°C

Given :  $a = 44.22 \text{ JK}^{-1} \text{ mol}^{-1}$ ,  $b = 8.79 \times 10^{-3} \text{ JK}^{-2} \text{ mol}^{-1}$ ,  $C = -8.02 \times 10^5 \text{ JK mol}^{-1}$ . 3+2

### CHT-13b

### Unit - I

Answer *any three* questions.

9. (a) State the two important deductions of Carnot's theorem.  
 (b) Prove both the deductions qualitatively. 2+3
10. (a) State the two famous statements of second law of thermodynamics by naming them properly.  
 (b) Show that both the statements are equivalent. 2+3

11. (a) What is Clausius Inequality?  
(b) A certain mass of ideal gas expands into vacuum to twice its initial volume. Calculate  $\Delta U$  and  $\Delta S$  of the process. 2+3
12. (a) Using Maxwell's relations derive the equation of state :  $\left(\frac{\partial H}{\partial P}\right)_T = -T\left(\frac{\partial V}{\partial T}\right)_P + V$   
(b) Define Joule-Thomson effect and Inversion temperature. 2+3
13. (a) Differentiate between Joule-Thomson cooling and adiabatic cooling.  
(b) Draw S-T diagram of a Carnot cycle labelling the diagram, mentioning properly all the processes involved. 2+3

### Unit - II

Answer *any two* questions.

14. (a) The half-life period of a first-order reaction is 15 min. Calculate the rate constant and time taken to complete 80% of the reaction.  
(b) What is a pseudo first-order reaction? Explain with an appropriate example. 2+3
15. (a) What is homogeneous catalysis? Explain with a suitable example.  
(b) Rate constants of a reaction at 300 K and 310 K are  $4.5 \times 10^{-5} \text{ sec}^{-1}$  and  $9.0 \times 10^{-5} \text{ sec}^{-1}$  respectively. Evaluate the activation energy and pre-exponential factor of the reaction. What should be the order of this reaction? 2+3
16. (a) Calculate the activation energy of a reaction, whose rate constant gets tripled by a rise of temperature from 22°C to 32°C.  
(b) Derive the Michaelis-Menten equation for enzyme catalysis explaining all the terms involved. 2+3
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